

Hybrid dimensional two phase flow in fractured porous media

K. Brenner^a, J. Hennicker^{a,b}, R. Masson^a, P. Samier^b

^a*Laboratoire de Mathématiques J.A. Dieudonné, UMR 7351 CNRS, University Nice Sophia Antipolis, and team COFFEE, INRIA Sophia Antipolis Méditerranée, Parc Valrose 06108 Nice Cedex 02, France*

^b*CSTJF, TOTAL S.A. - Avenue Larribau, 64018 Pau, France*

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In this work, we extend the single phase Darcy flow model proposed in [1], [2] to two phase flow. We thus provide a model for two phase Darcy flow through discrete fracture networks (DFN) in porous media, in which the $d - 1$ dimensional flow in the fractures is coupled with the d dimensional flow in the matrix, leading to the so called hybrid dimensional Darcy flow model.

The model accounts for fractures acting either as drains or as barriers, since it allows pressure jumps at the matrix-fracture interfaces. The model also permits to treat gravity dominated flows as well as discontinuous capillary pressure curves at the material interfaces.

The discretization is based on an adaptation of the Vertex Approximate Gradient (VAG) and Hybrid Finite Volume schemes to this problem, in order to account for anisotropy and heterogeneity aspects as well as for applicability on general polyhedral meshes.

The numerical analysis for the single phase flow model is carried out in an extended gradient schemes framework (see [2]). In so doing, we obtain error estimates and prove convergence, which has not been achieved before for flow in complex DFN.

For two phase flow, we present several test cases including gravity and capillary effects (see Figures 1,2,3 below). The VAG scheme is used to compare our hybrid dimensional model to the hybrid dimensional, continuous pressure model (proposed in [3]) and to the generic equidimensional model, in which fractures have the same dimension as the matrix. This does not only provide quantitative evidence about computational gain, but also leads to deep insight about the quality of the proposed reduced model.

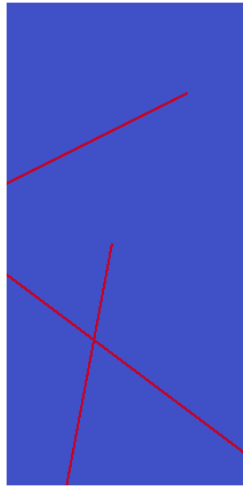


Figure 1: 2D test case with three fractures. The reservoir is initially saturated with water and oil is injected in the bottom fracture.

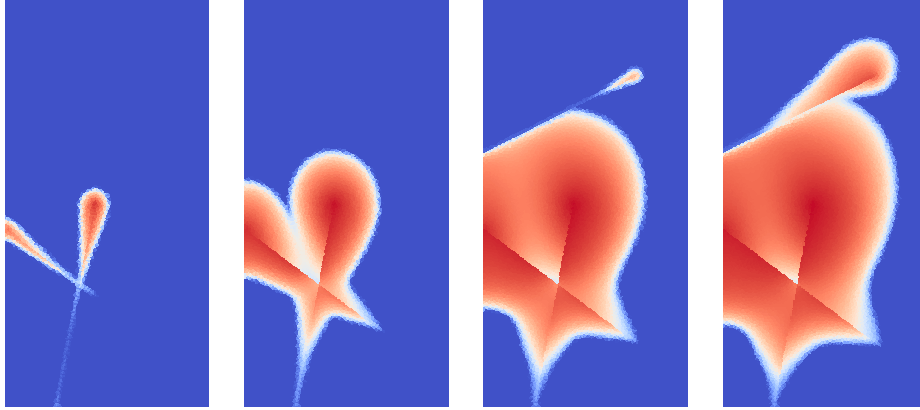


Figure 2: Oil saturation in the reservoir obtained at successive times for our reduced model and for a gravity dominant flow with the three fractures acting as drains. The capillary pressure is zero in the fractures and given by $P_c(S^o) = -10^5 \ln(1 - S^o)$ in the matrix.

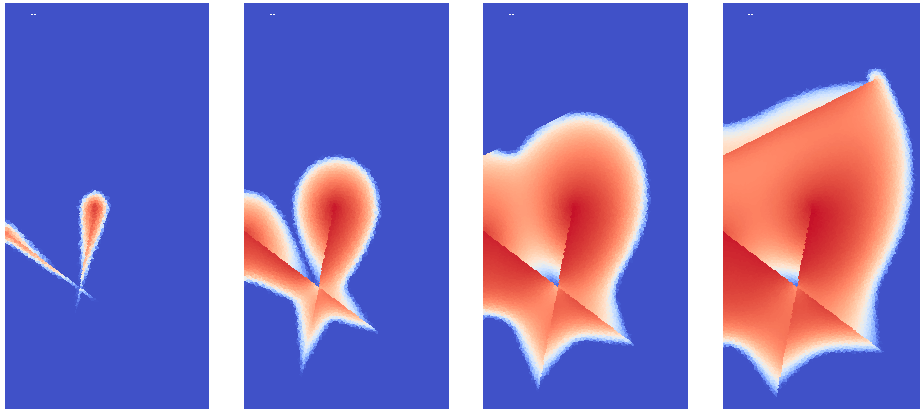


Figure 3: Oil saturation in the reservoir obtained at successive times for our reduced model and for a gravity dominant flow with the two bottom fractures acting as drains and the top fracture acting as a barrier. The capillary pressure is zero in the two bottom fractures and given by $P_c(S^o) = -10^5 \ln(1 - S^o)$ in both the top fracture and the matrix.

References

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